Dynamic Neural Units and Genetic Algorithms With Applications to the Optimal Control of Nonlinear Systems

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요 약

"Dynamic Neural Unit"(DNU) based upon the topology of a reverberating circuit in a neuronal pool of the central nervous system. In this thesis, we present a genetic DNU-control scheme for unknown nonlinear systems. Our method is different from those using supervised learning algorithms, such as the backpropagation (BP) algorithm, that needs training information in each step. The contributions of this thesis are the new approach to constructing neural network architecture and its trainings.

1. Introduction:

Control refers to a task which is to apply appropriate inputs to a plant so that the plant performs in a desirable way. In practical, many control problems suffer from difficulty due to system nonlinearity, uncertainty, and dynamic property. The existing control methods are system specific; i.e., a control methodology designed for a type of nonlinear system may not be suitable for other types of nonlinear systems, while neural networks can approximate arbitrary nonlinear functions. A neuro-control system, in general, performs a specific form of adaptive control, with the controller taking the form of multilayer neural network and the adaptable parameters being defined as the adjustable connection weights which could be better adapt to different plant and environmental conditions.

The "dynamic neural units"(DNUs) which have been proposed by professors M.M.Gupta and D.H.Rao with a different architecture to model a new artificial neuron that enables both the synaptic and somatic adaptations to control the nonlinear system.

In this paper, we present a dynamic neural network(DNN) that created by DNUs to control the nonlinear system, and give an assume of using Genetic algorithms(GA) to optimize the parameters of the network weights.

2. The Dynamic Neural Units (DNUs)

We know that biological neuron provides two distinct mathematical operations distributed over the synapse and soma of neuron. From the biological point of view, the two operations of them are physically separate, however, in the modeling of biological neuron, they have been combined.

The dynamic neural unit (DNU), whose topology embodies delay elements,
feedforward and feedback synaptic weights, and a nonlinear operator has been used successfully for controlling unknown linear and nonlinear dynamic systems by considering only the synaptic weights as the adjustable parameters of the network. The topology of a single dynamical neural unit consists of delay elements, feedback and feedforward synaptic weights and a nonlinear somatic operator. The architecture of the DNU model is illustrated in Fig 1.[1] 

Fig.1. Basic structure of DNU, which consists of synaptic and somatic components.

\[ x(0) \in R^r \rightarrow v_i(x) = v_i(x_{in}, au, bw)x(0) \]
\[ u(x) = \Psi [g, g, v_i] \]

Fig.2. Symbolic representation of DNU.

The difference equation that describes the behavior of the second order dynamical structure is given in Eqn. (1) in which \( v_1(k), x(k) \). Similarly, the pulse transfer function of this part can be given by Eqn. (2).

\[ v_i(k) = -b_1v_i(k-1) + b_2v_i(k-2) + a_0x(k) + a_1x(k-1) + a_2x(k-2) \]

(1)

\[ T(z) = \frac{a_0 + a_1 z^{-1} + a_2 z^{-2}}{1 + b_1 z^{-1} + b_2 z^{-2}} \]

(2)

The output of the DNU can be evaluated as follows;

\[ v(k) = g, v_i(k) \]

(3)

\[ u(k) = \Psi (v(k)) = \tanh(g, v_i(k)) \]

(4)

The objective is based on the minimization of the instantaneous error evaluated at the output of the system. The cost function that is to be minimized is defined by Eqn.(6) in which \( E \) denotes the expectation operator. If \( \omega \) denotes the parameters of a single DNU, the update rule can be given by:

\[ w_{k+1} = w_k - \mu \frac{\partial J}{\partial w} \]

(5)

\[ J = \frac{1}{2} E(e^2(k)) \]

(6)

\[ e(k) = y_s(k) - u(k) \]

(7)

More compactly, the parameter update rule is given by Eqns (8) (9) (10) where \( i = 0,1,2 \) and \( j = 1,2 \):

\[ \Delta a_i(k+1) = u_{a_i} E(e(k)g_{s_i}(k)sec h^2[v_i(k)]x(k-i)) \]

(8)

\[ \Delta b_i(k+1) = u_{b_i} E(e(k)g_{s_i}(k)sec h^2[v_i(k)]v_i(k-j)) \]

(9)

\[ \Delta g_{s_i}(k+1) = g_{s_i}(k)u_{g_{s_i}} E(e(k)sec h^2[v_i(k)]v_i(k)) \]

(10)

In the parameter update equations, the coefficients \( u_{a_i}, u_{b_i} \) and \( u_{g_{s_i}} \), denote the step size for the corresponding parameter and are chosen to be constant throughout a simulation.

3. The Dynamic Neural Network (DNN) control model:

In Fig. 3, DNU layer includes the desired number of individual DNU blocks whose inputs are connected together and whose outputs are added to form the control \( u(k) \). Depending on the magnitude of the output error, the algorithm updates the feedforward and feedback weights and the gain of the nonlinear activation functions of each dynamical neural unit in the DNU layer. The derivation of the algorithm is given in [1] in detail.

Figure 3. Control scheme for a nonlinear dynamic system using dynamic neural network

In our example, we adopt a three-stage dynamic neural network, an input stage, an intermediate stage, and an output stage is formed. In each stage there are two DNU with a weight connect to next stage in each DNU. The DNN structure is showed in fig.4.
4. Applied Genetic Algorithm to adjust the parameters of the DNN:

Genetic algorithms have been utilized for many control problems. P. Wang et al. presented a numerical example in which a pH (potential of hydrogen) neutralization process is regulated by a PID controller with its parameters optimized using simple GA[2]: A. Varek et al. employed GA to derive control rules[3] encoded as decision tables and to optimize the parameters of the induced rules. Some researchers also studied genetically optimized fuzzy logic control[4][5][6]. In their study, GAs played a role of optimizing membership functions and fuzzy linguistic rule sets. W. Schiffmann et al. introduced GAs to optimize the BP algorithm for training multilayer neural networks [7].

4.1 Genetic Algorithm

Genetic Algorithm (GA) is a random technique that imitates natural evolution with Darwinian survival of the fittest approach. GAs perform the coding of the parameters and not on the exact parameters, therefore, it does not depend on the continuity of the parameter nor the existence of derivatives of the functions as needed in some conventional optimization algorithms. The coding method allows GAs to handle multi-parameters or multi-model type of optimization problems easily, which is rather difficult or impossible to be treated by classical optimization methods[8].

The population strategy enables GA to search the near optimal solutions from various parts and directions within a search space simultaneously. Therefore, it can avoid converging to the local minimum or maximum points better. GA processes each chromosome independently and makes it highly adaptable for parallel processing. It needs no more than only the relative fitness of the chromosomes, thus, it is rather suitable to be applied to systems that are ill-defined. GAs can also work well for non-deterministic system or systems that can only be partially modeled. GAs use random choice and probabilistic decision to guide the search, where the population improves toward near optimal points from generation to generation.

GAs consists of three basic operations: reproduction, crossover, and mutation. Reproduction is the process where members of the population reproduced according to the relative fitness of the individuals, where the chromosomes with higher fitness have higher probabilities of having more copies in the coming generation. There are a number of selection schemes available for reproduction, such as ‘roulette wheel’, ‘tournament scheme’, ‘ranking scheme’, etc. [9][10]. Crossover in GA occurs when the selected chromosomes exchange partially their information of the genes, i.e., part of the string is interchanged within two selected candidates. Mutation is the occasionally alteration of states at a particular string position. Mutation is essentially needed in some cases where reproduction and crossover alone are unable to offer the global optimal solution. It servers as an insurance policy which would recover the loss of a particular piece of information. Further discussion on GAs can be obtained in [9][10].

4.2 Tuning of the DNN Parameters by GA:

The steps optimizing parameters of DNN by GA is as follows:

Coding strategy of the DNN parameters: a total of 42 parameters (6DNUs + 6variables + 6weights) are needed to be tuned by GA. Each of the parameters is encoded into 8-bit string, resulted in a complete chromosome of 336 bits.

Initial populations comprise a set of chromosome: in this experiments, the population consists of 200 chromosomes which are all randomized initially.

Optimization by GA: the process is shown in fig. 5:

Fig. 5 A functional block diagram showing the GA optimization process.

The terminal condition of the GA optimization process is to determine a bounded control input $u(k)$ such that:
$$\lim_{k \to \infty} |y_d(k) - y(k) - e(k)| = 0 \quad (k: \text{the steps of the GA optimization process})$$
4. Computer Simulation Results:

In our simulations, we applied this model to control of an unknown nonlinear plant. The plant to be controlled is an arbitrary unknown function:

\[ f(x) = 2 + \cos(7 \times (y_2(k-1) + y_2(k-2))) + e - u(k)/1 + u_2(k-1) + u_2(k-2); \]

The input to the system is \( x(k) = \sin(2 - k/250) \) in the interval [-1,1].

In this experiment, the input signal \( x(k) \) is considered the desired response for the unknown nonlinear plant to follow.

The simulation result of the typical DNN is shown as Fig.6,7 [1], and our simulation result of the same DNN using GA optimized algorithm is shown as Fig.8,9,10.

From these figures, we could see whether the typical DNN model or the DNN with GA controlled the plant response follows the desired command signal closely.

5. Conclusion:

This paper has presented a Dynamic Neural Network (DNN) where all its parameters be simultaneously tuned by Genetic Algorithm (GA). By appropriate coding of the DNN parameters, it can achieve self-tuning properties from an initial random state. By using of dynamic crossover and mutation probability rates, the tuning process by GA was further improved. Though it not better than typical DNN controller, and can be argued that in this model, before GA can be used to optimize its parameters, initial encoding and setting are required, however, such procedures are somewhat relatively simpler, and could widely be used.

Fig.6 Error Signal of typical DNN
Fig.7 Plant Output of typical DNN

Fig.8 The Input and Nonlinear Signal
Fig.9 The DNN Output signal Using GA

Fig.10 The Error Signal of DNN Using GA

6. REFERENCES

[1] M.M. Gupta, D.H. Rao, "Dynamic Neural Units with Applications to the Control of Unknown Linear System", in *Journal of Intelligent and Fuzzy Systems*, pp.73–92, vol.1, no.1

